

# a brief history of

bla k  
holes

*andreas müller*

*theory group max camenzind  
lsw heidelberg*

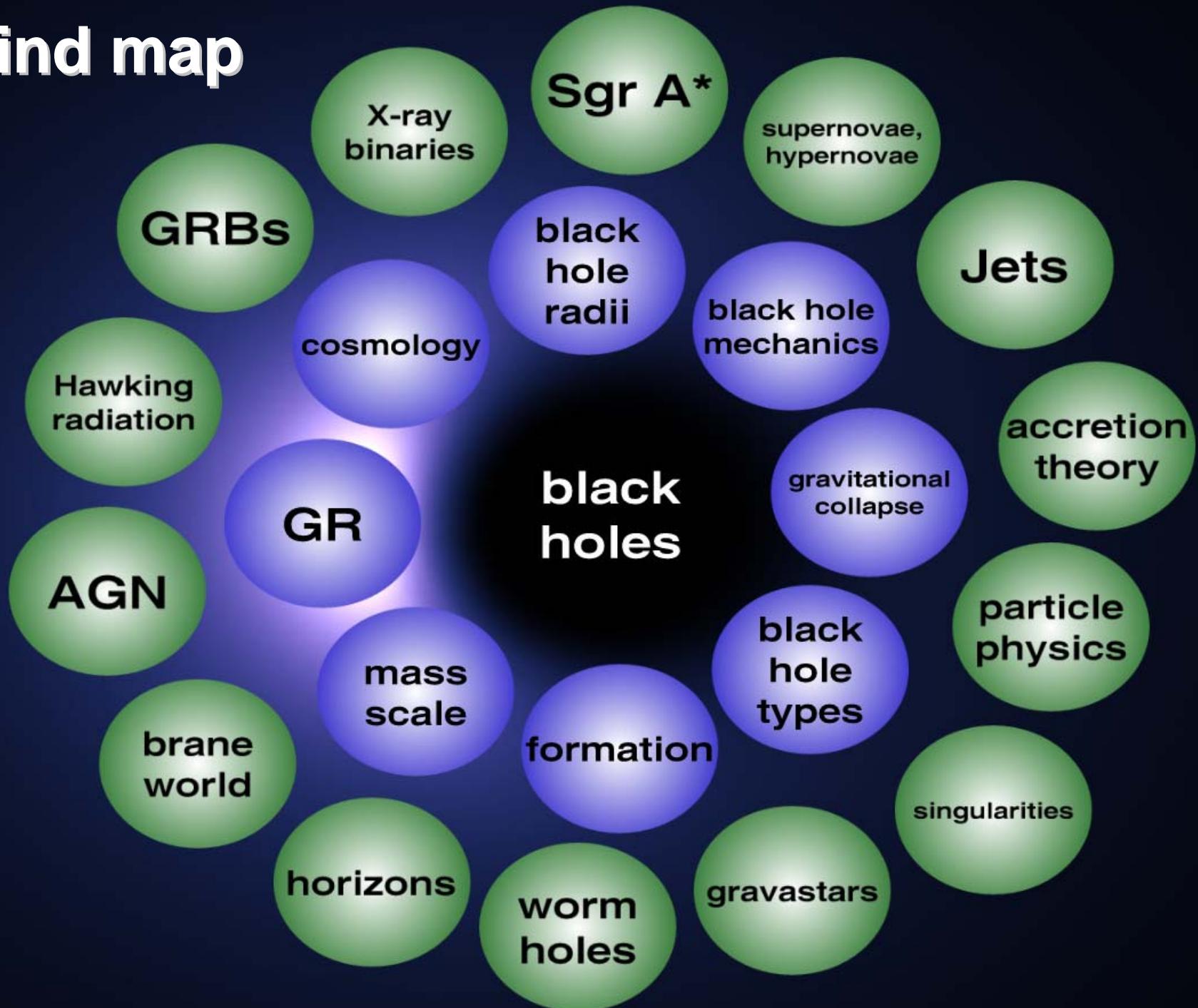
<http://www.lsw.uni-heidelberg.de/users/amueller>

*student seminar  
mpia & lsw  
january 2004*

# talk organisation

- basics 😊
- standard knowledge
- advanced knowledge
- edge of knowledge and verifiability 💀

# mind map



# what is a black hole?

*black*



*escape velocity c*

*hole*



*singularity in space-time*

notion „*black hole*“ from relativist *john archibald wheeler* (1968),  
but first speculation from geologist and astronomer *john michell* (1783)



# black holes in relativity

- solutions of the vacuum field equations of einsteins general relativity (1915)

$$G_{\mu\nu} = 0$$

- some history:

➤ schwarzschild	1916 (static, neutral)
➤ reissner-nordstrøm	1918 (static, electrically charged)
➤ kerr	1963 (rotating, neutral)
➤ kerr-newman	1965 (rotating, charged)

- all are petrov type-d space-times
- plug-in metric  $g_{\mu\nu}$  to verify solution ;-)
- black hole mass hidden in (point or ring) singularity



# black holes have no hair!



*maximal set:*  
 $\{M, a, Q\}$

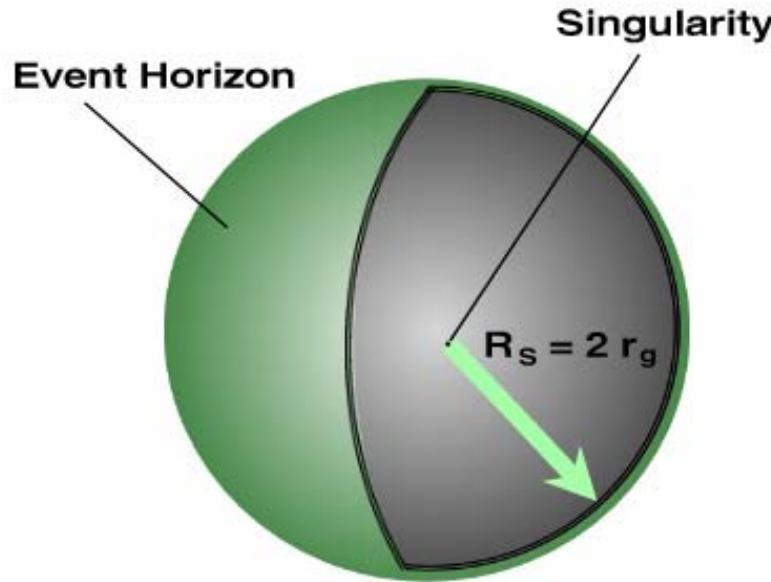
- schwarzschild  
 $\{M\}$
- reissner-nordstrom  
 $\{M, Q\}$
- kerr  
 $\{M, a\}$
- kerr-newman  
 $\{M, a, Q\}$

*wheeler: no-hair theorem*



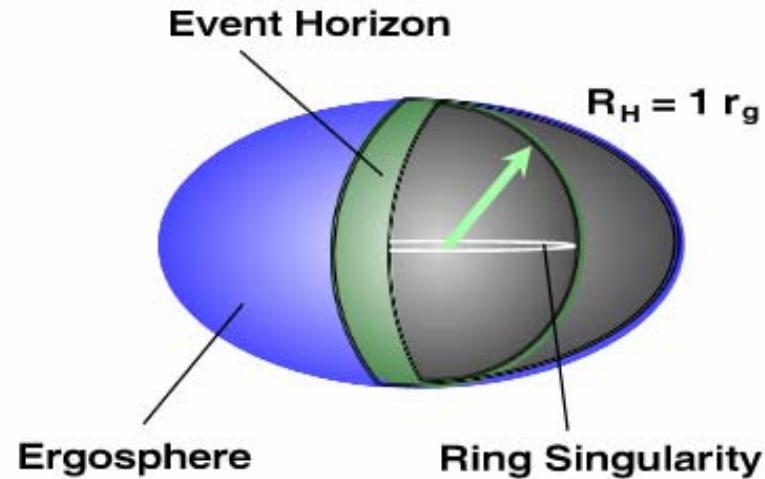
# black holes – schwarzschild vs. kerr

## Black Holes



**Schwarzschild**

$$a = 0$$



**Kerr**

$$a = 1$$



# black holes – kerr in boyer-lindquist

$$ds^2 = -\alpha^2 dt^2 + \tilde{\omega}^2(d\Phi - \omega dt)^2 + (\rho^2/\Delta) dr^2 + \rho^2 d\Theta^2$$

$$\alpha = \frac{\rho\sqrt{\Delta}}{\Sigma}$$

black hole mass  $M$   
spin parameter  $a$

$$\Delta = r^2 - 2Mr + a^2$$

$$\rho^2 = r^2 + a^2 \cos^2 \theta$$

$$\Sigma^2 = (r^2 + a^2)^2 - a^2 \Delta \sin^2 \theta$$

$$\omega = \frac{2aMr}{\Sigma^2}$$

$$\tilde{\omega} = \frac{\Sigma}{\rho} \sin \theta$$

lapse function

delta potential

generalized radius

sigma potential

frame-dragging frequency

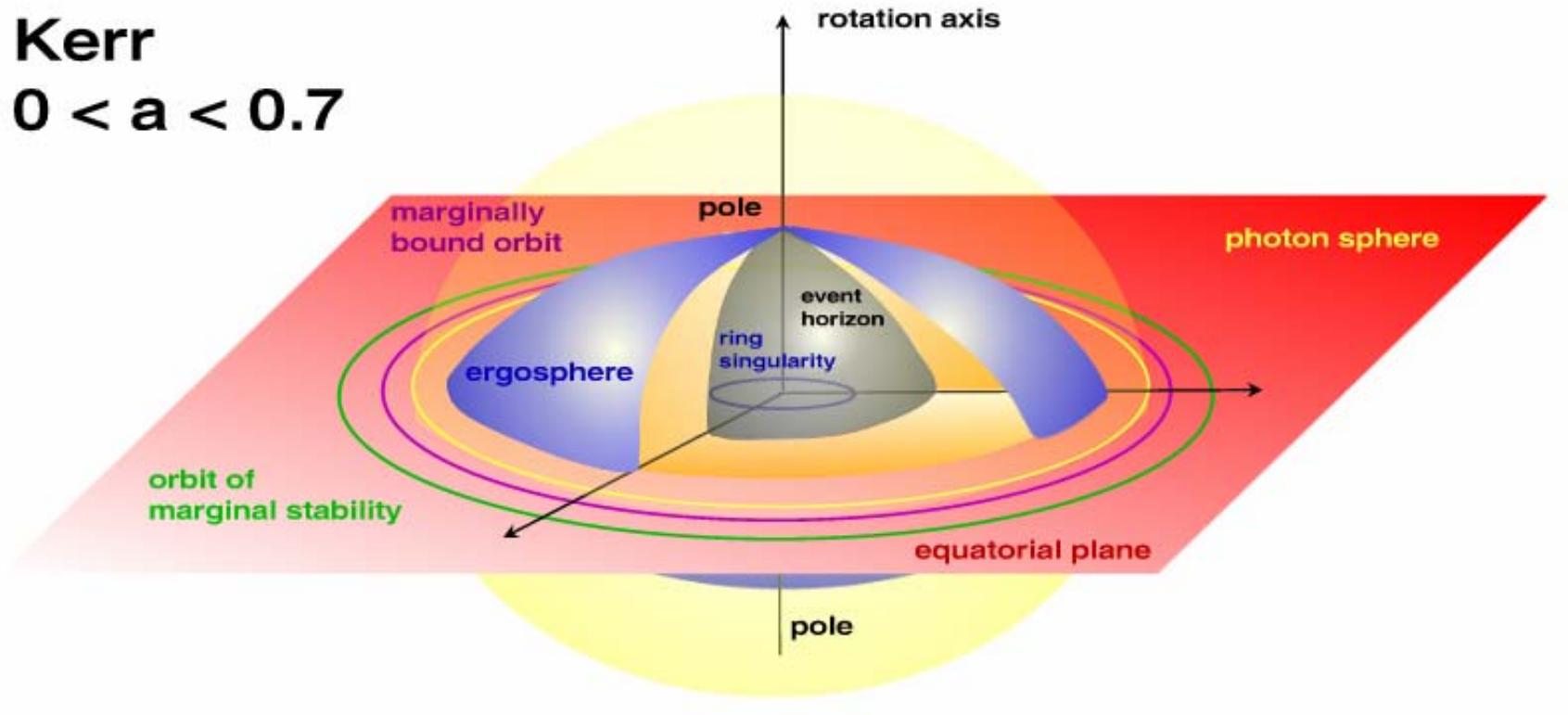
cylindrical radius



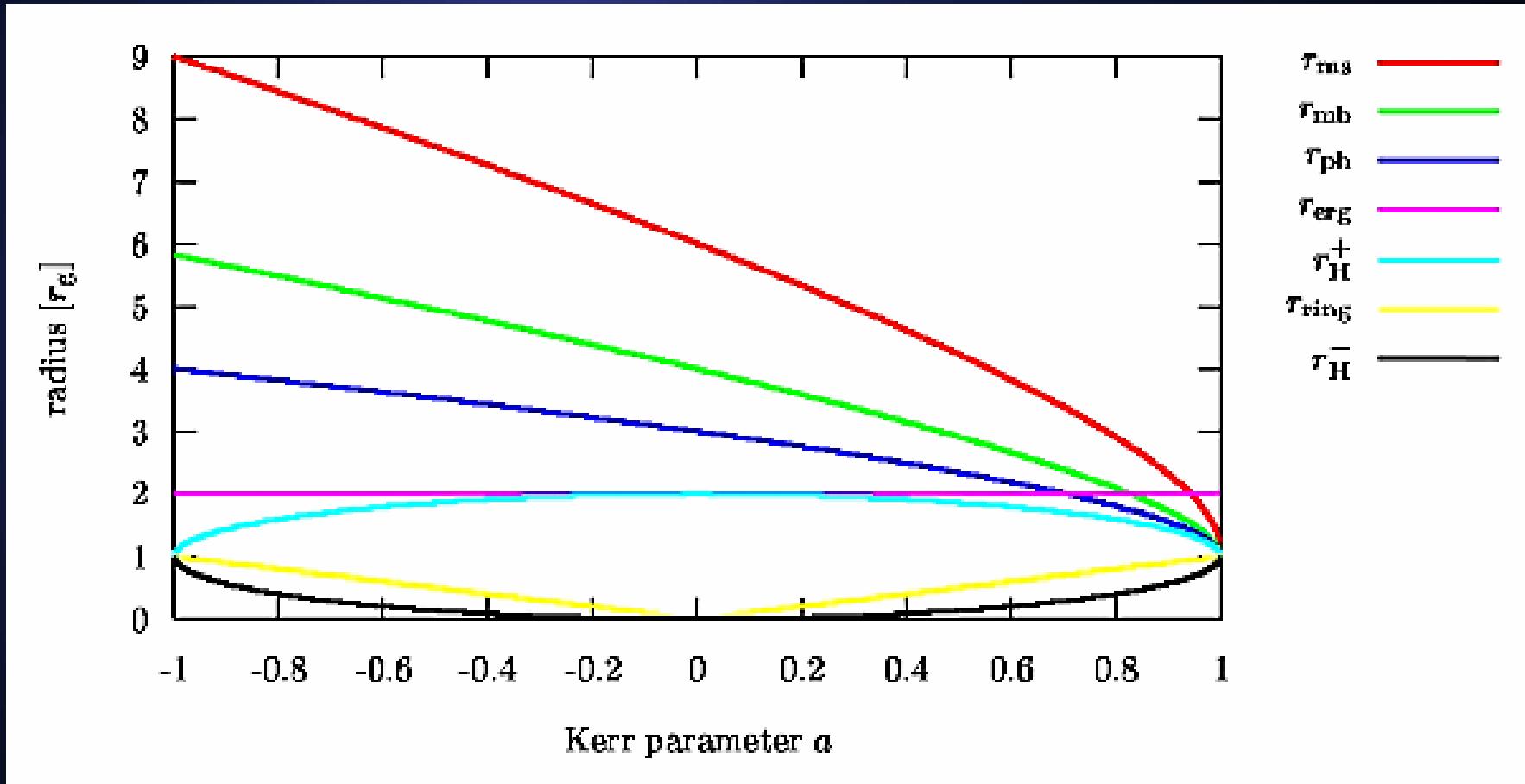
# black hole topology

Kerr

$0 < a < 0.7$

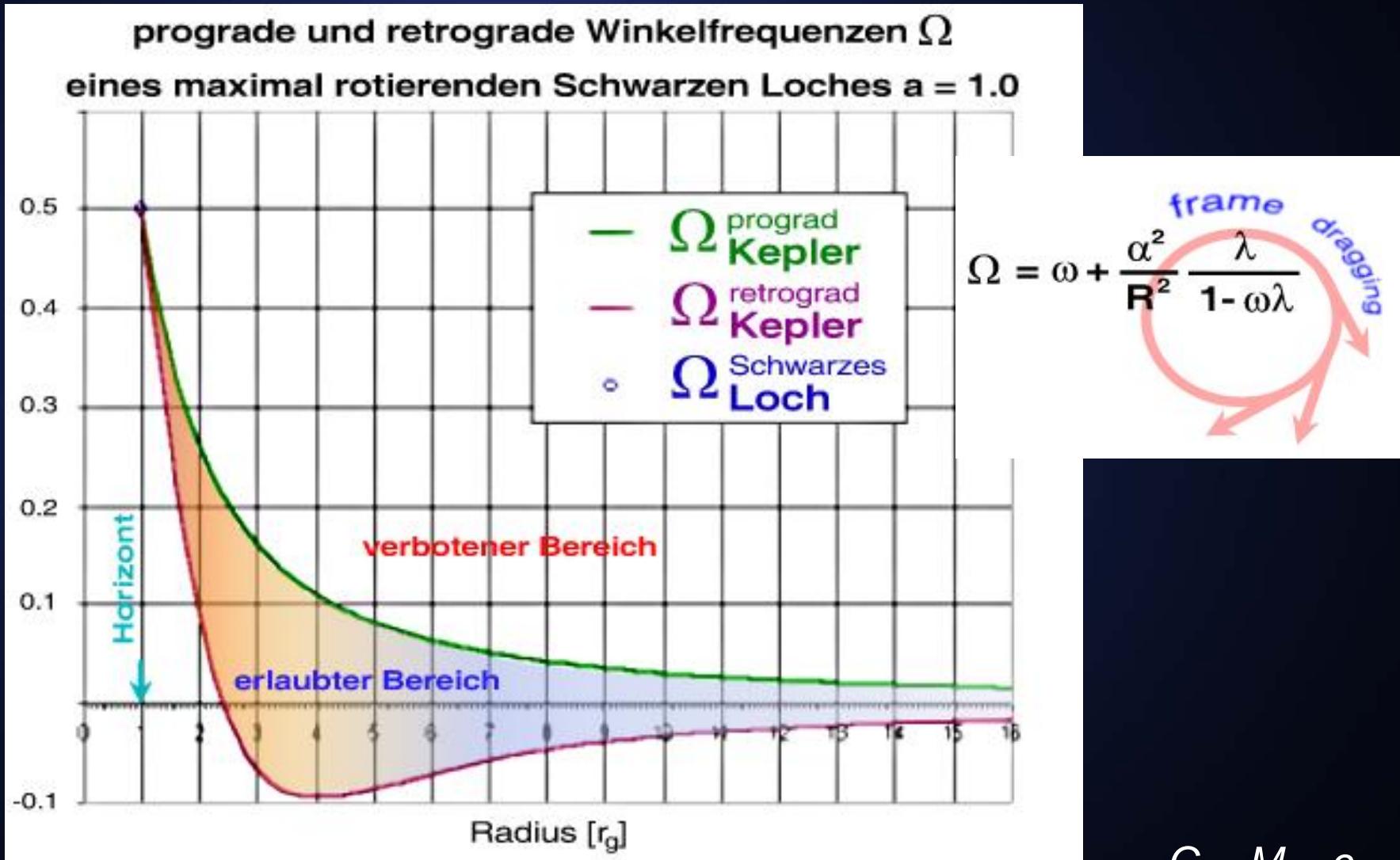


# black hole – characteristic radii



$$G = M = c = 1$$

# black hole - frame drag



# black holes – mass scale

- |                |   |
|----------------|---|
| ■ TeV          | $M_{BH} \sim 1 \text{ TeV}$                   |
| ■ primordial   | $M_{BH} \sim 10^{18} \text{ g}$               |
| ■ stellar      | $1 M_{\odot} < M_{BH} < 100 M_{\odot}$        |
| ■ massive      | $100 M_{\odot} < M_{BH} < 10^5 M_{\odot}$     |
| ■ supermassive | $10^5 M_{\odot} < M_{BH} < 10^{10} M_{\odot}$ |
- 
- |                |   |
|----------------|---|
| ■ TeV          | mini holes in particle accelerators (?) |
| ■ primordial   | early universe, galactic seeds (?)      |
| ■ stellar      | fate of massive stars, microquasars     |
| ■ massive      | globular clusters (?)                   |
| ■ supermassive | galactic centers and agn                |

stellar bh indicators: hypernovae, grbs, supernovae  
supermassive bh indicators: M- $\sigma$  relation

# black hole formation

- TeV relativistic heavy ion collisions?
- primordial hen-egg problem...  
brill waves  
topological defects after ssb?
- stellar gravitational collapse  
supernova type Ia: exploding wd  
ns-ns merging  
ns-bh merging
- massive accreting black holes  
cluster merging?  
popIII vms relics?  
podourets-zel'dovich instabilities
- supermassive accreting black holes  
podourets-zel'dovich instabilities  
galaxy merging

in principle all types (?): super-critical brill waves

# black hole from stellar collapse

## Stars

*hydrostatical equilibrium*

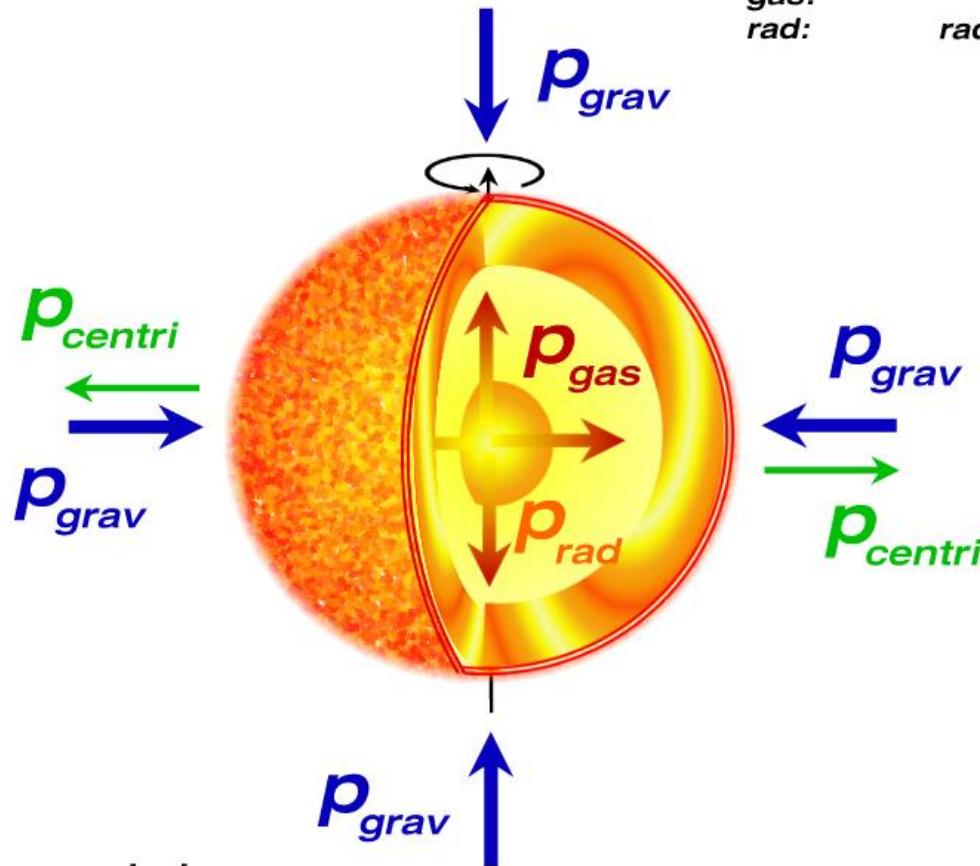
*pressure species:*

*grav:* gravitational

*centri:* centrifugal

*gas:* gas

*rad:* radiative



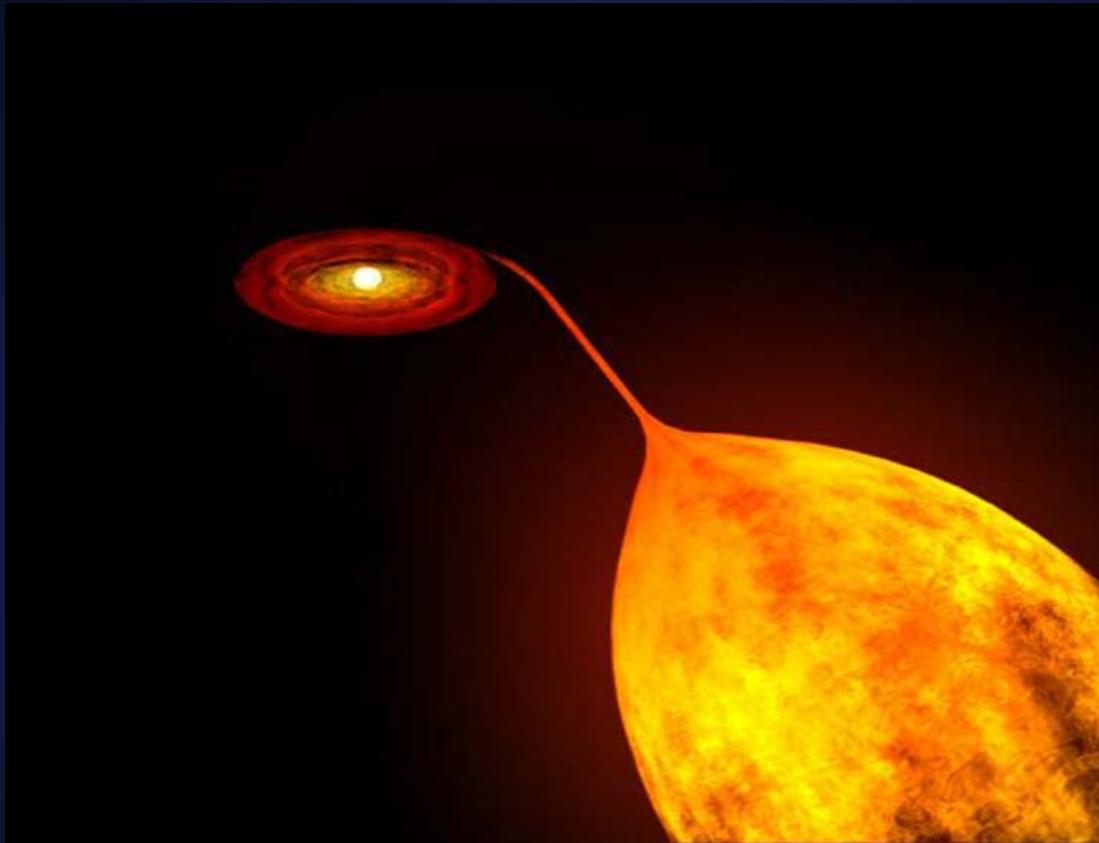
*pressure balance:*

$$p_{grav} = p_{centri} + p_{gas} + p_{rad}$$

# black hole from stellar collapse

- canonical scenario:  
gravitational collapse of massive stars
- $M_{\text{progenitor}} > 1.65 M_{\odot}$  (*burgio et al. 2001*)
- hydrostatic equilibrium:  $p_{\text{grav}} = p_{\text{centri}} + p_{\text{gas}} + p_{\text{rad}}$
- after silicon burning:  
thermonuclear burning chain breaks
- $p_{\text{rad}}$  and  $p_{\text{gas}}$  decrease rapidly  
 $\Rightarrow p_{\text{grav}} > p_{\text{centri}} + p_{\text{gas}} + p_{\text{rad}}$  **dominant gravitation!**
- star implosion and explosion from back-bounce:
  - $\Rightarrow$  supernovae, hypernovae (grbs)
  - $\Rightarrow$  stellar black hole
  - $\Rightarrow$  possibly detectable in a binary system

# black holes in x-ray binaries



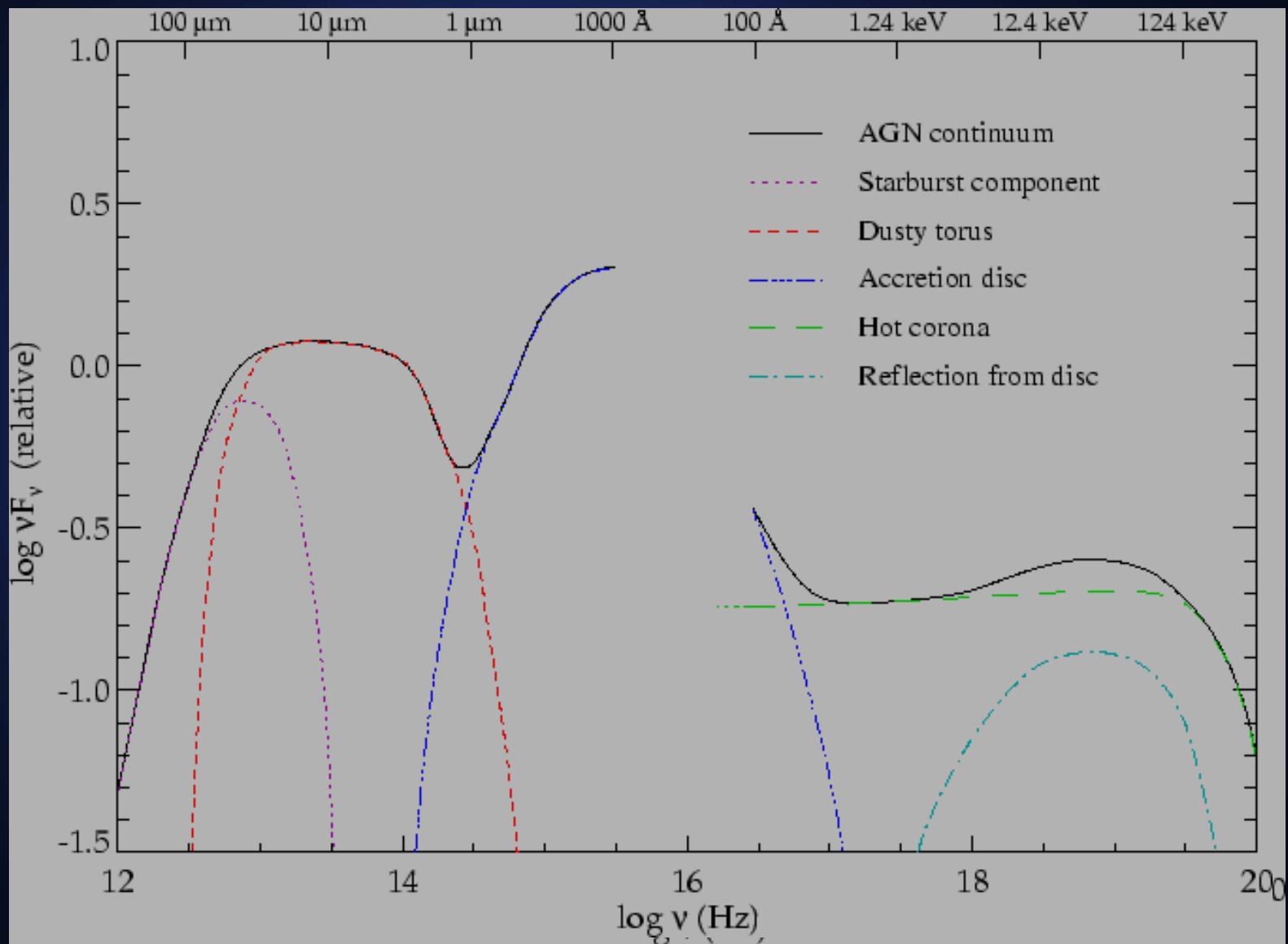
sketch,  
chandra homepage

- stellar black holes:  $1 M_{\odot} < M_{\text{BH}} < 100 M_{\odot}$
- roche lobe overflow through inner lagrange point
- hot accretion flow radiates x-rays
- spin-up to nearly extreme kerr,  $a \sim 1$ , by accretion of angular momentum

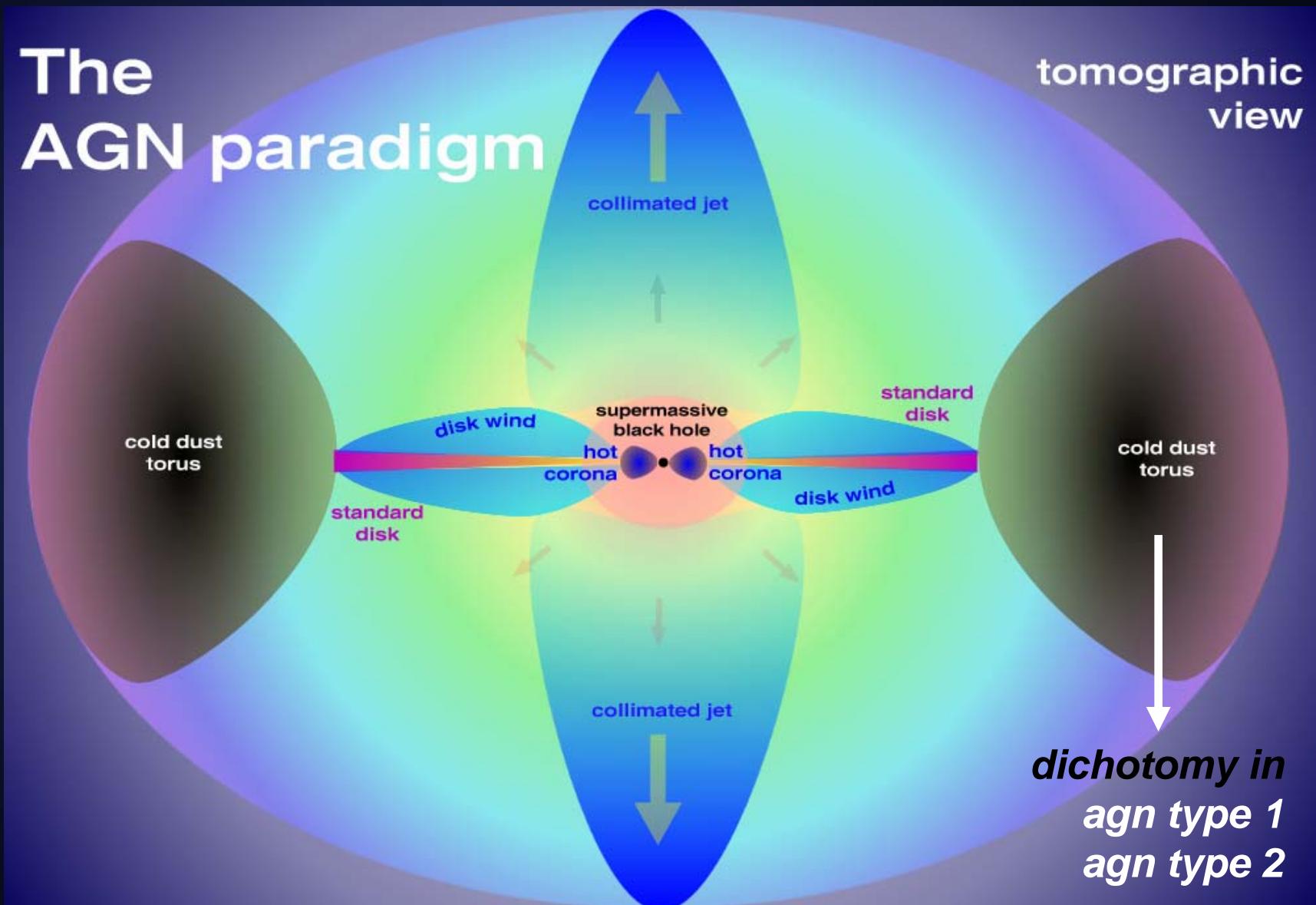
# black holes in agn

- engine of active galactic nuclei (agn):  
accretion onto a supermassive black hole  
(smbh) with typically  $M_{\text{BH}} > 10^5 M_{\odot}$
- accretion most efficient mechanism to transform  
gravitative binding energy into radiative energy
- eddington limit:  
$$L_{\text{edd}} = 4\pi\sigma_T^{-1}GM_{\text{BH}}m_p c$$
$$\sim 1.3 \times 10^{46} \text{ erg/s} \times M_{\text{BH}}/(10^8 M_{\odot})$$
- $R_S = 2 \text{ AU} \times M_{\text{BH}}/(10^8 M_{\odot})$
- typical agn luminosities:
  - $L_{\text{qso}} \sim 10^{47} \text{ erg/s}$
  - $L_{\text{seyf}} \sim 10^{43} \text{ erg/s}$

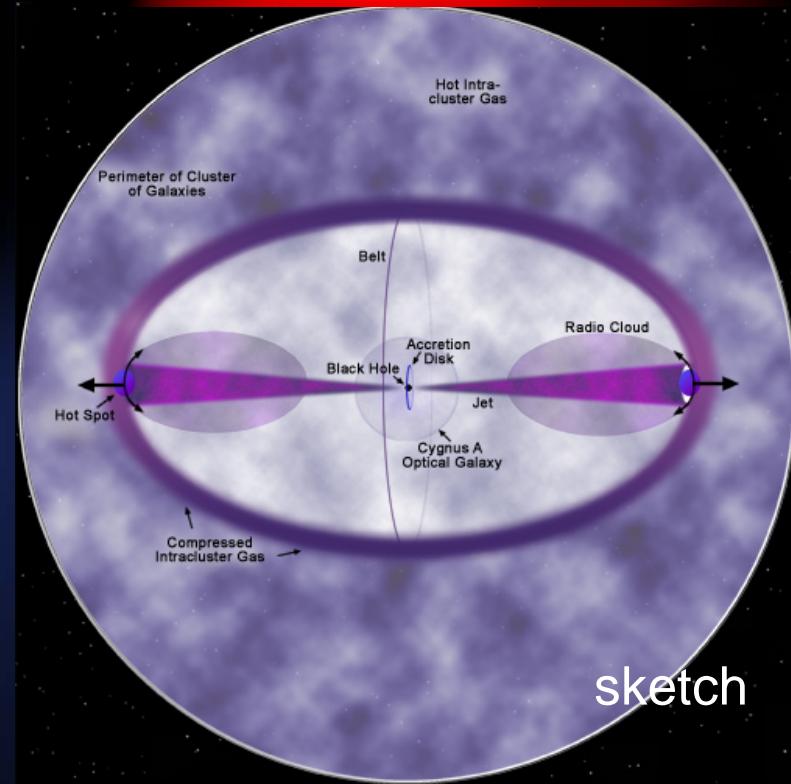
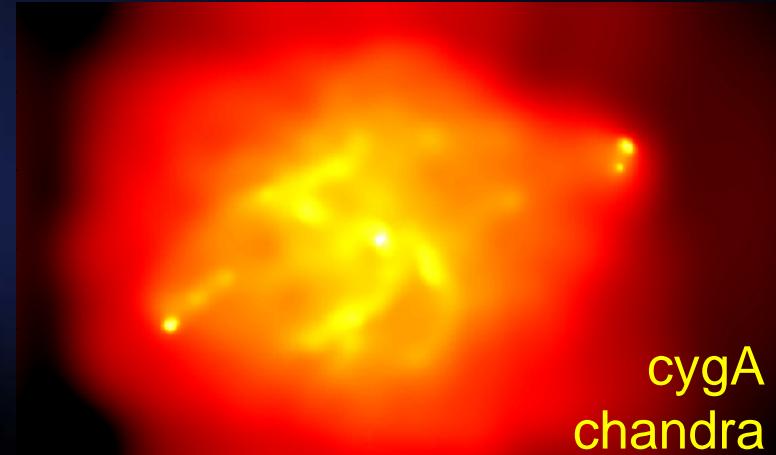
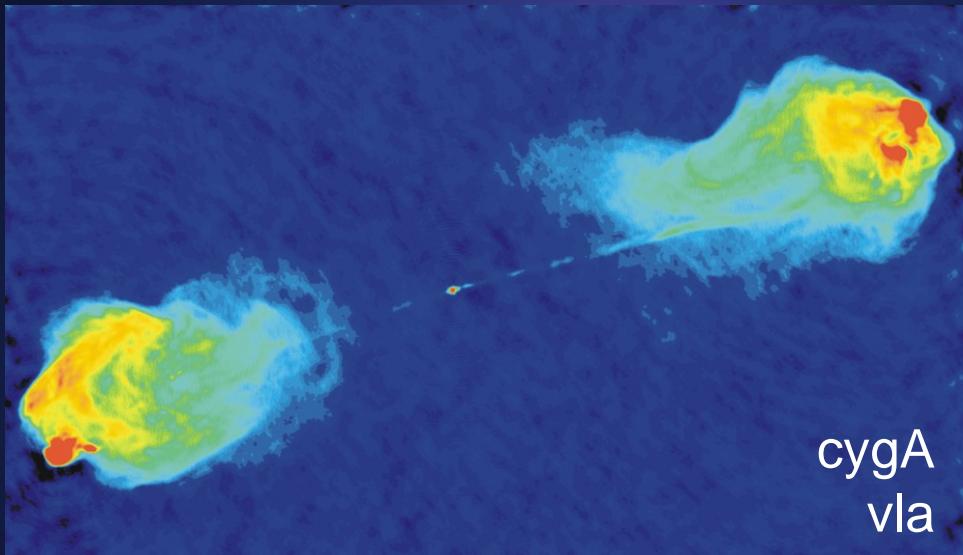
# agn triple bump spectra



# black holes and agn paradigm



# black holes in centers of galaxies and agn



- supermassive black holes:  
 $M_{BH} > 10^5 M_{\odot}$
- growth on accretion time scale
- spin-up to nearly extreme kerr,  
 $a \sim 1$ , by accretion of angular momentum

# black holes in centers of galaxies: sgr a\*

- compact radio source sgr a\*
- radio synchrotron emission from thermal and non-thermal  $e^-$  distributions in compact region
- gravitomagnetic dynamo effects in black hole magnetosphere: dominantly toroidal B-field at  $r_{ms}$
- sub-mm bump
- nuclear star cluster of massive stars and x-ray binaries (lmxbs, magnetic cvs) on 1“ scale
- sgr a\* associated with supermassive black hole  
 $2.6 \times 10^6 M_\odot < M_{BH} < 4.8 \times 10^6 M_\odot$

# black holes in centers of galaxies: sgr a\*

- bh mass determination by tracking keplerian orbits of
  - stars (innermost star is up to now S2)
  - nir flares (keck: *ghez et al. 2003*, vlt: *genzel et al. 2003*)
  - x-ray flares (chandra: *baganoff et al. 2001, 2003*, xmm: *porquet et al. 2003*), brandnew: astro-ph/0401589
- nir and x-rax flares (duration min-h)
  - ⇒ evidence for black hole rotation:  $0.5 < a < 1$
- nature of flaring object?
- GC dimness:  $L_x \sim 10^{33}$  erg/s
  - strong gravity (gravitational redshift) at  $r_{ms}$   
(aschenbach *et al. 2004*)
  - low accretion rate
  - radiatively-inefficient accretion flows (*yuan et al. 2003*),
  - cold inactive disks (*sunyaev et al. 2003*)

# black holes in centers of galaxies: M - $\sigma$ relation

- velocity dispersion  $\sigma$  in galactic bulge hints for compact dark object (cdo): the supermassive black hole (smbh)
- stellar motion, stellar gas disks, masers in galactic bulge are tracers for velocity dispersion
- observational tool: spectroscopy with a slit
- M –  $\sigma$  relation:

$$\log(M_{\text{CDO}}/M_\odot) = \alpha + \beta \log(\sigma/\sigma_0)$$

- $(\alpha; \beta) \sim (8.13; 4.02)$  with  $\sigma_0 = 200$  km/s
- M –  $\sigma$  relation is an estimator for SMBH determinations in galaxies and AGN

# black holes in centers of galaxies: M - $\sigma$ relation

- ❖ stellar kinematics
- △ gas kinematics
- \* maser kinematics
- ↖ nuker measurements

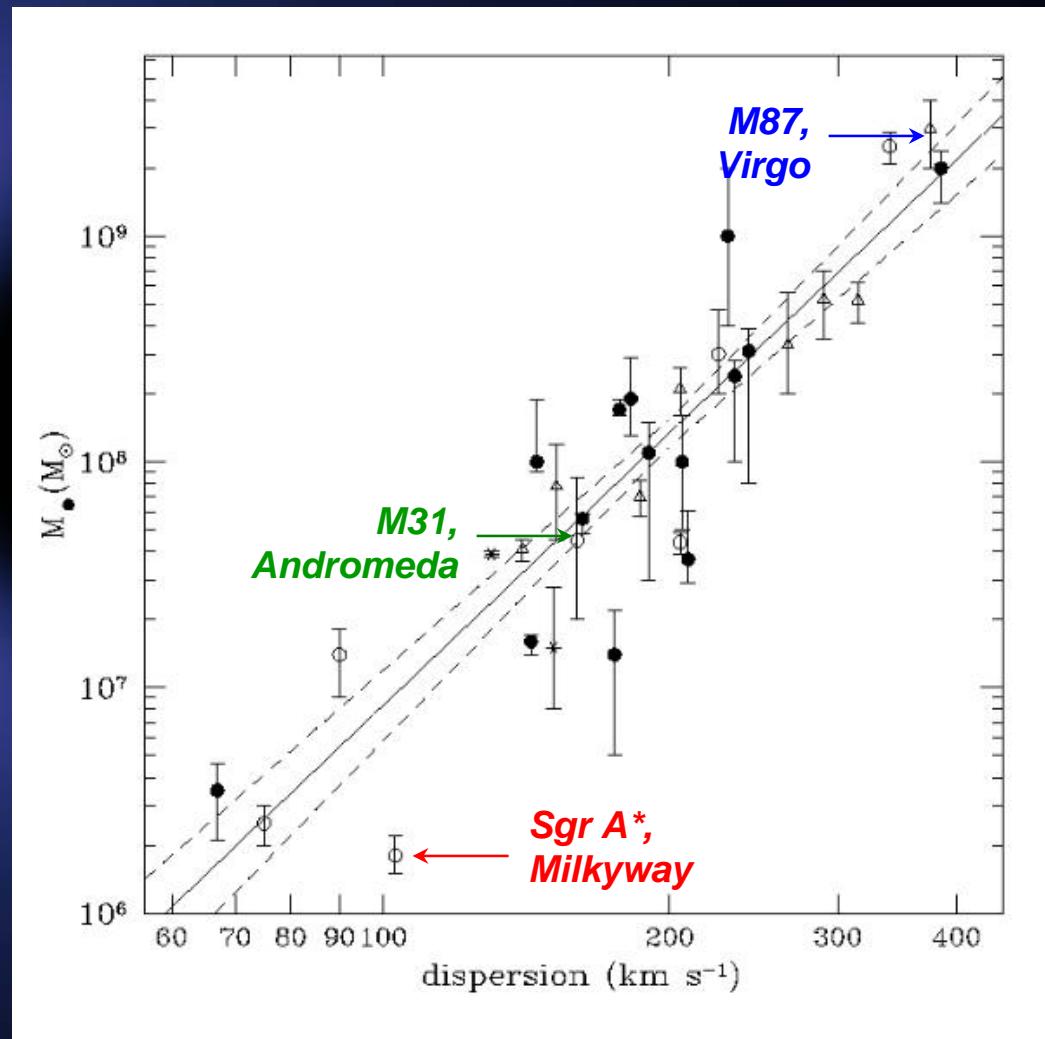
solid:

best fit  $\alpha = 8.13$ ,  $\beta = 4.02$

dashed:

$1\sigma$

$$M \sim \sigma^4$$

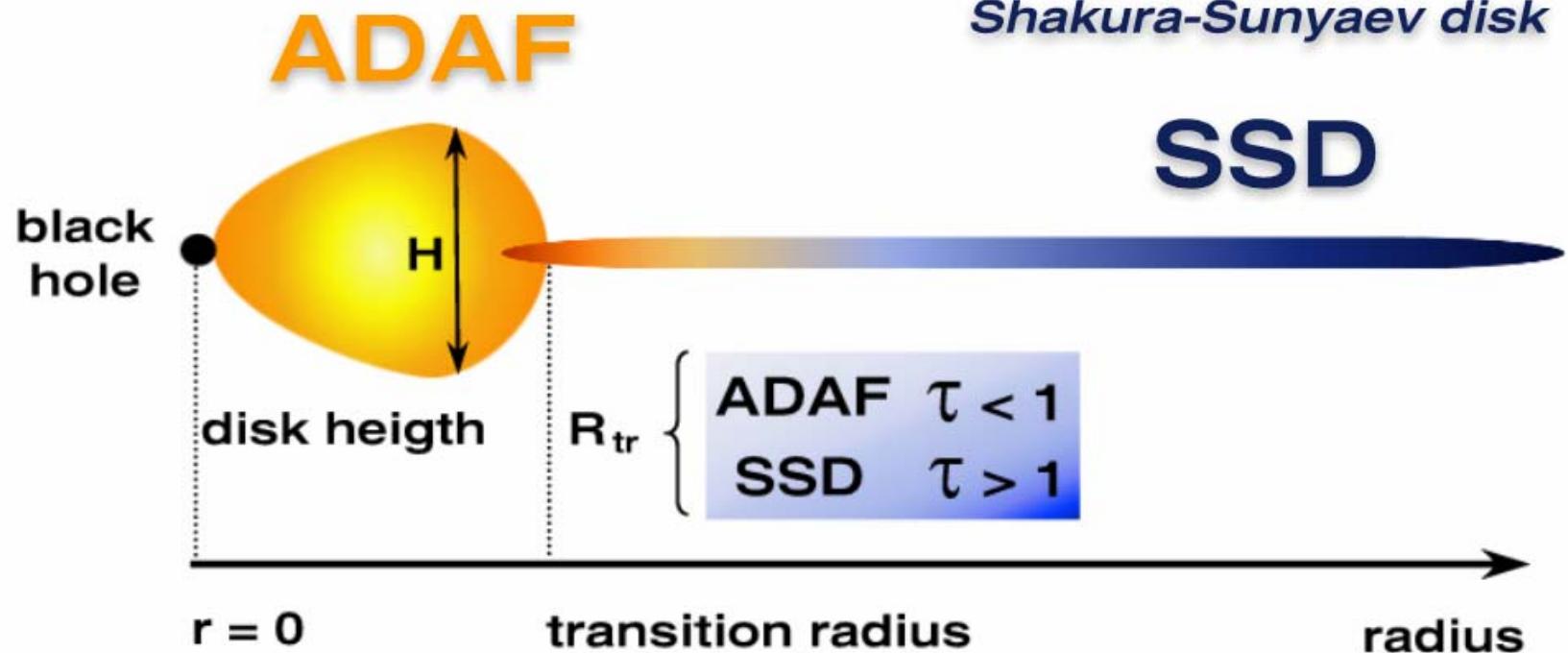


# accreting black hole simulation

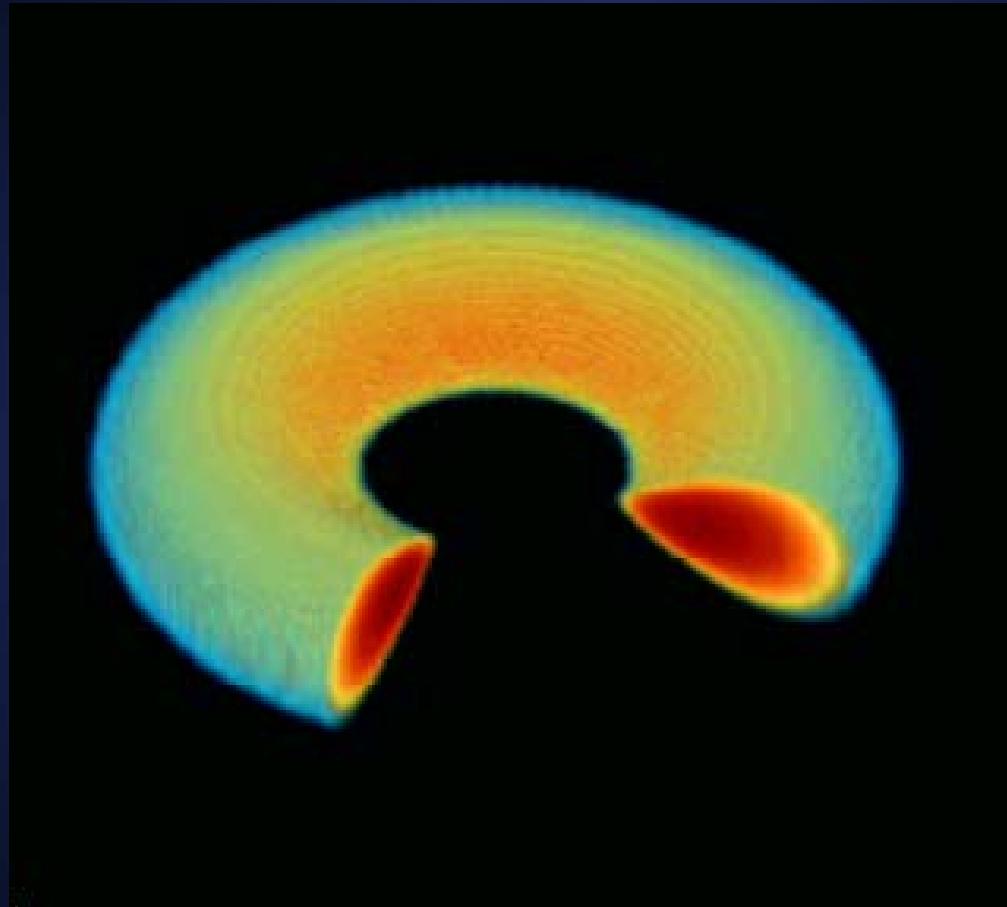
- background metric:  
pseudo-newtonian, schwarzschild, kerr
- hydrodynamics (hydro)
- magnetohydrodynamics (mhd)
- 2d, 2.5d, 3d
- ideal (euler), resistive or dissipative (navier-stokes)
- numerical techniques:
  - finite difference (fdm)
  - finite volume (fvm)
  - finite element (fem)
- numerical relativity: adm formalism (3+1 split)
- canonical approach: start with well-defined torus solution and simulate time evolution of this object (decay via turbulence, mri)
- co-ordinate systems: boyer-lindquist, kerr-schild
- challenge: boundary at the horizon

# accreting black holes - ssd

*advection-dominated accretion flow*



# accreting pseudo black holes



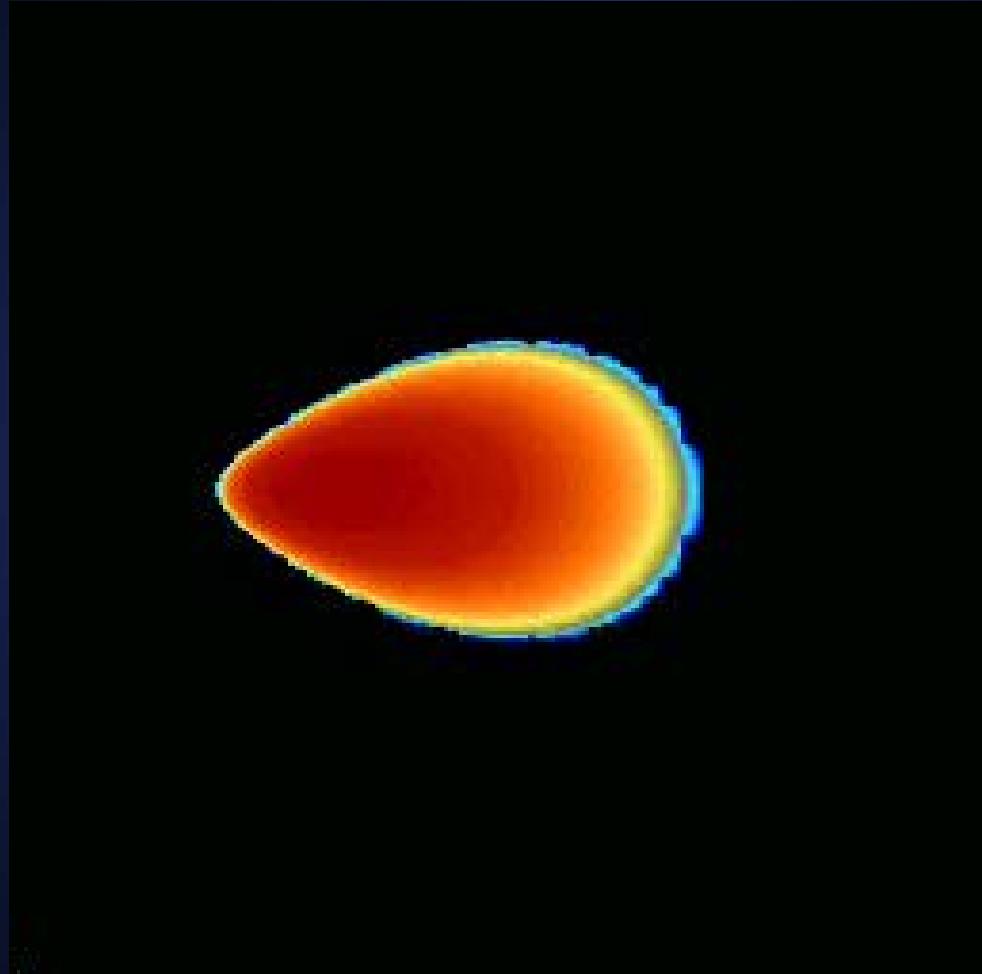
- pseudo-newtonian  
(paczynski-wiita potential)

$$\Phi = -\frac{GM}{r - r_g}$$

- 3D ideal mhd
- mhd turbulence
- magneto-rotational instability (mri)
- large-amplitude waves at  $r_{ms}$

*hawley & krolik 2001,*  
<http://www.astro.virginia.edu/VITA/papers/pndisk/pndisk.html>

# accreting black holes - grmhd



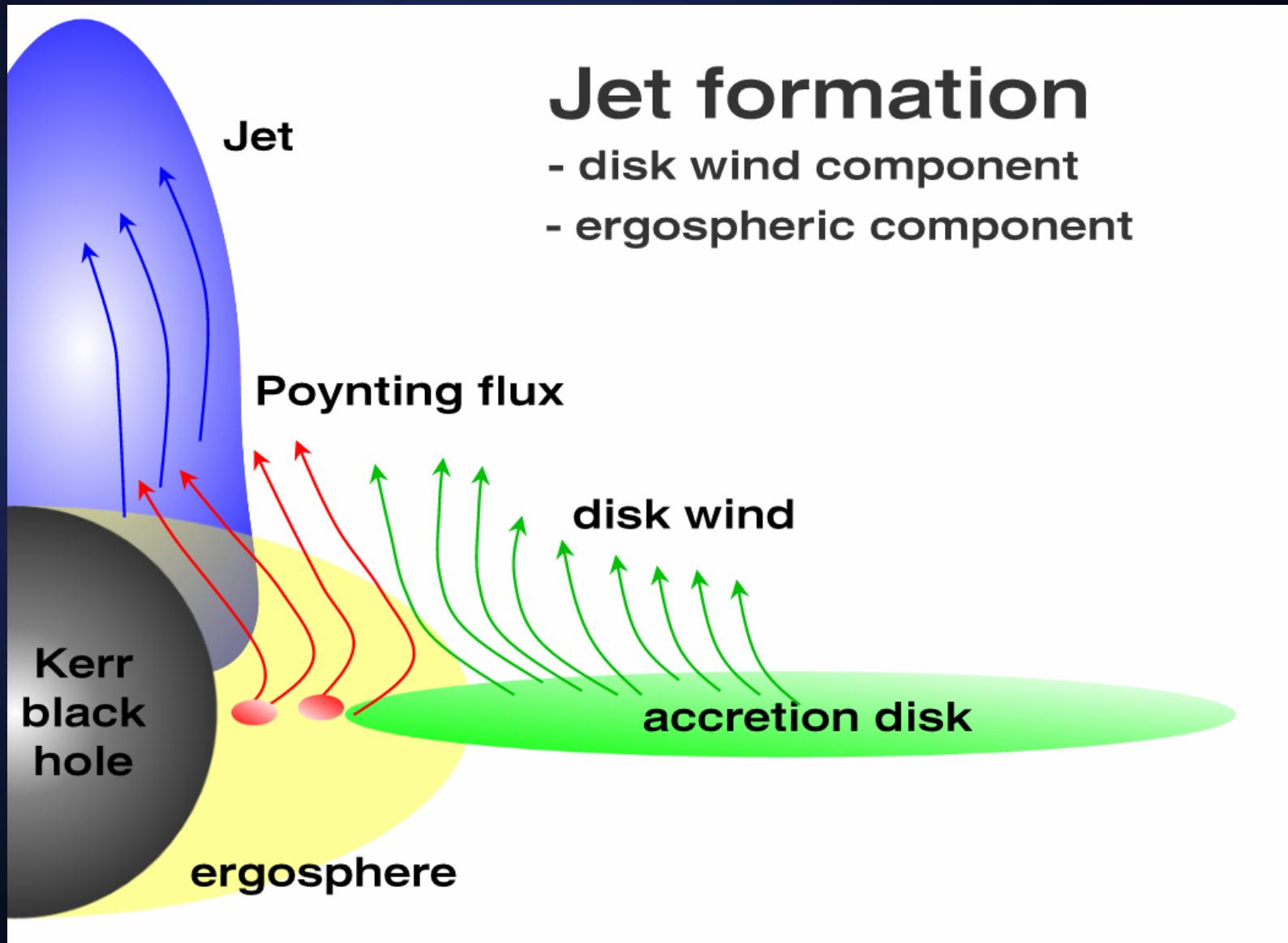
- 3D grmhd on kerr
- initial torus configuration
- mhd turbulence
- magneto-rotational instability (mri)
- initial magnetic field in poloidal loops,  $\beta = 100$
- movie: 10 orbits at  $p_{\max}$
- gas density shown

*de villiers & hawley 2003,*  
[http://www.astro.virginia.edu/~jd5v/KD\\_movies.htm](http://www.astro.virginia.edu/~jd5v/KD_movies.htm)

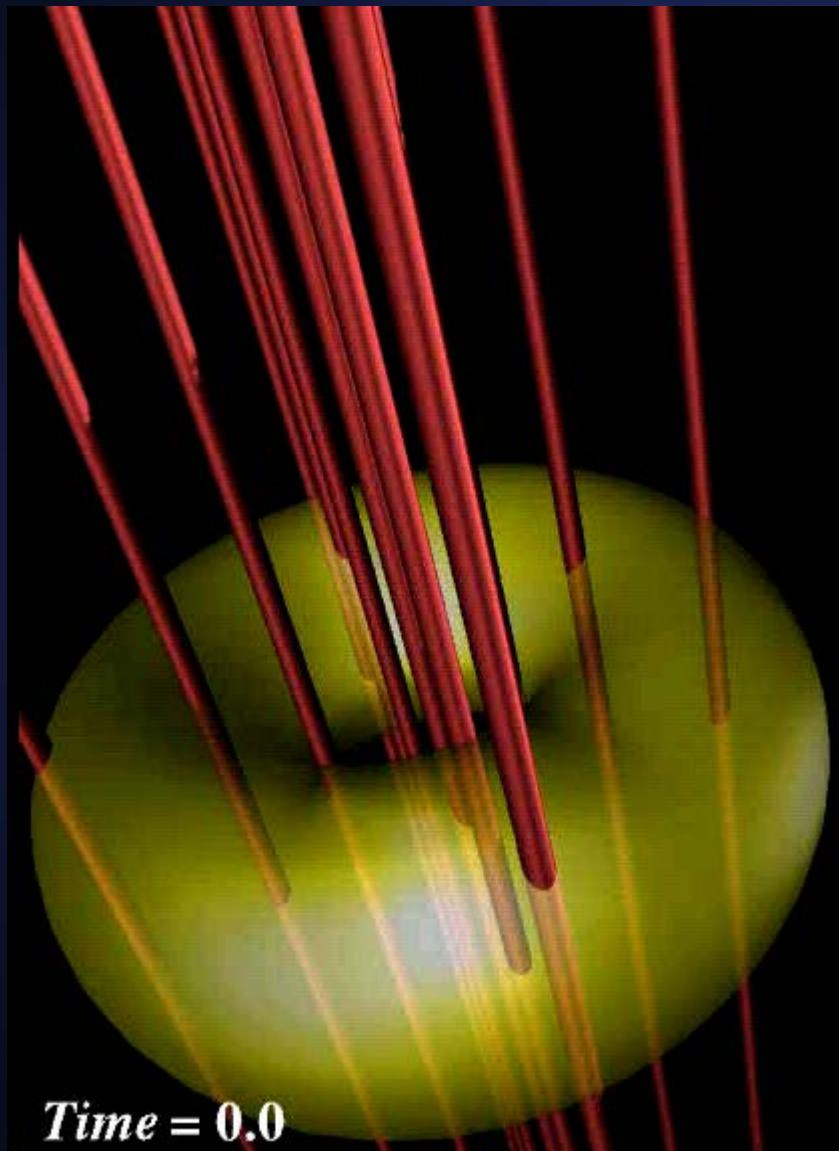
# accreting black holes - challenges

- accretion theory gives solution
  - shakura-sunyaev disk (ssd)
  - advection-dominated accretion flow (adaf)
  - non-radiative accretion flow (nraf)
- nraf on kerr investigated  
*(koide, shibata et al. 2001, de villiers & hawley 2003)*
- trouble-shooting
  - radiatively cooled solutions
  - radiation transfer in curved space-time
  - neutrino cooling

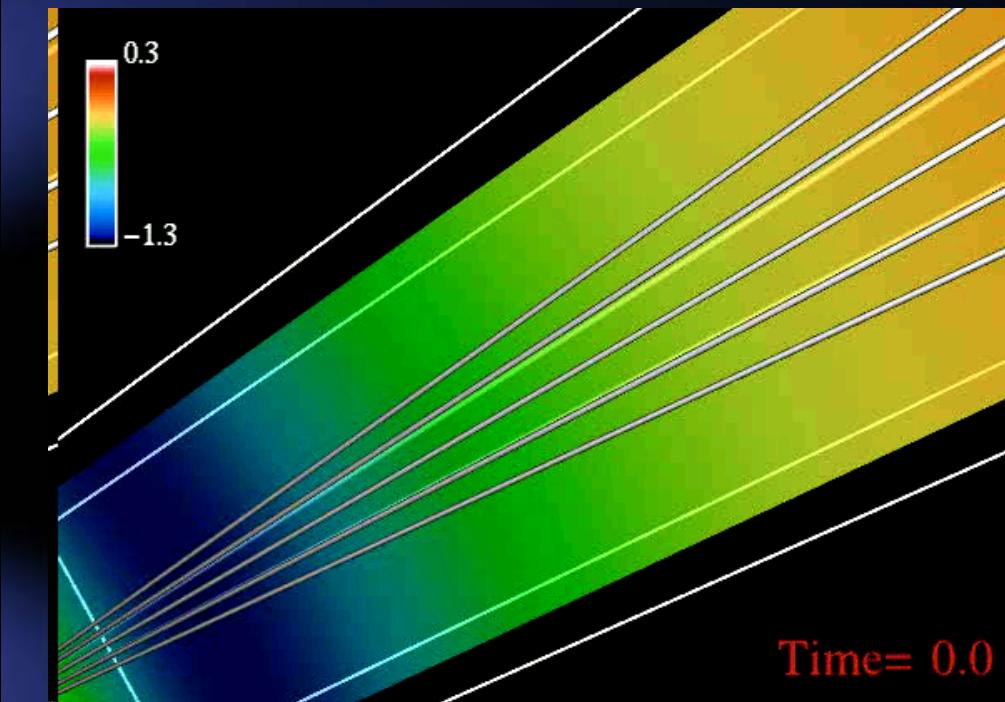
# black holes – jet-disk symbiosis



# black holes – mhd jet launching

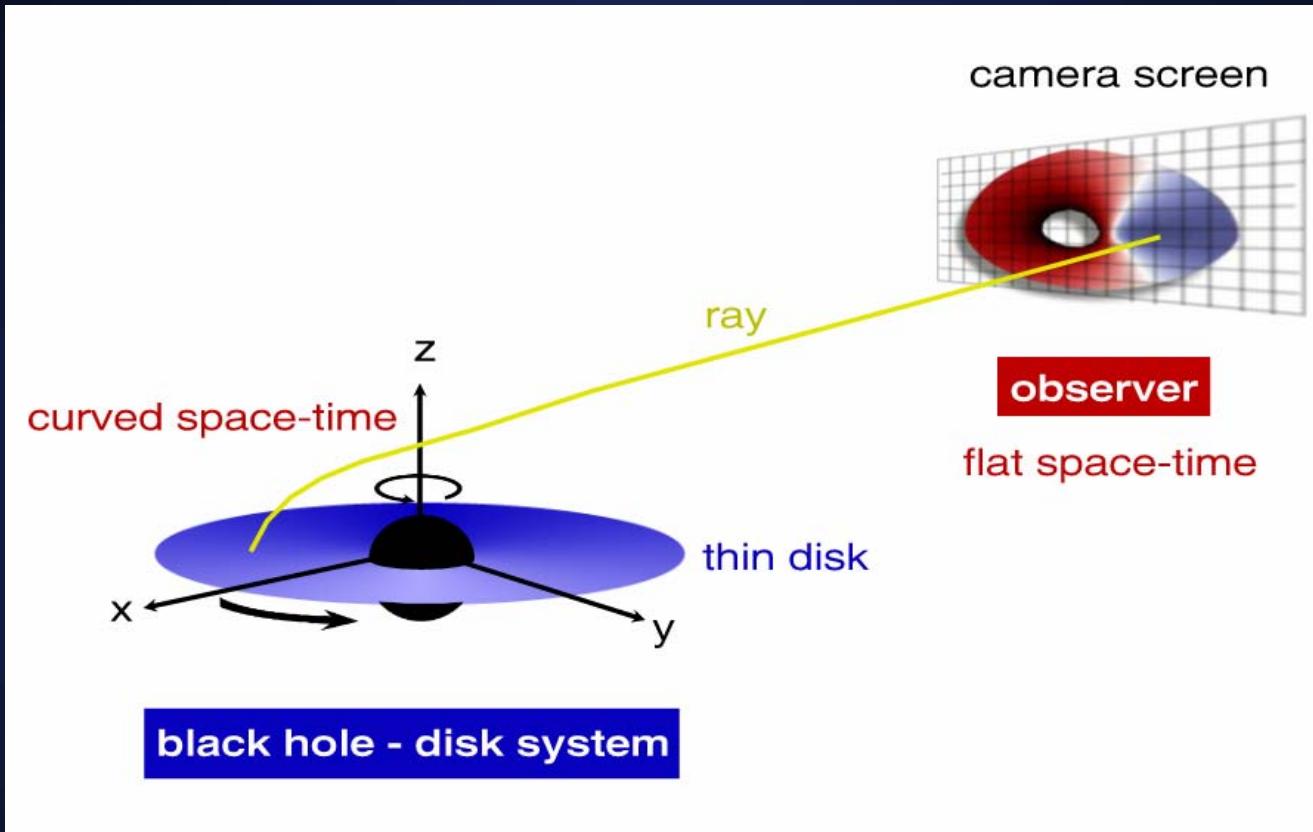


*Time = 0.0*



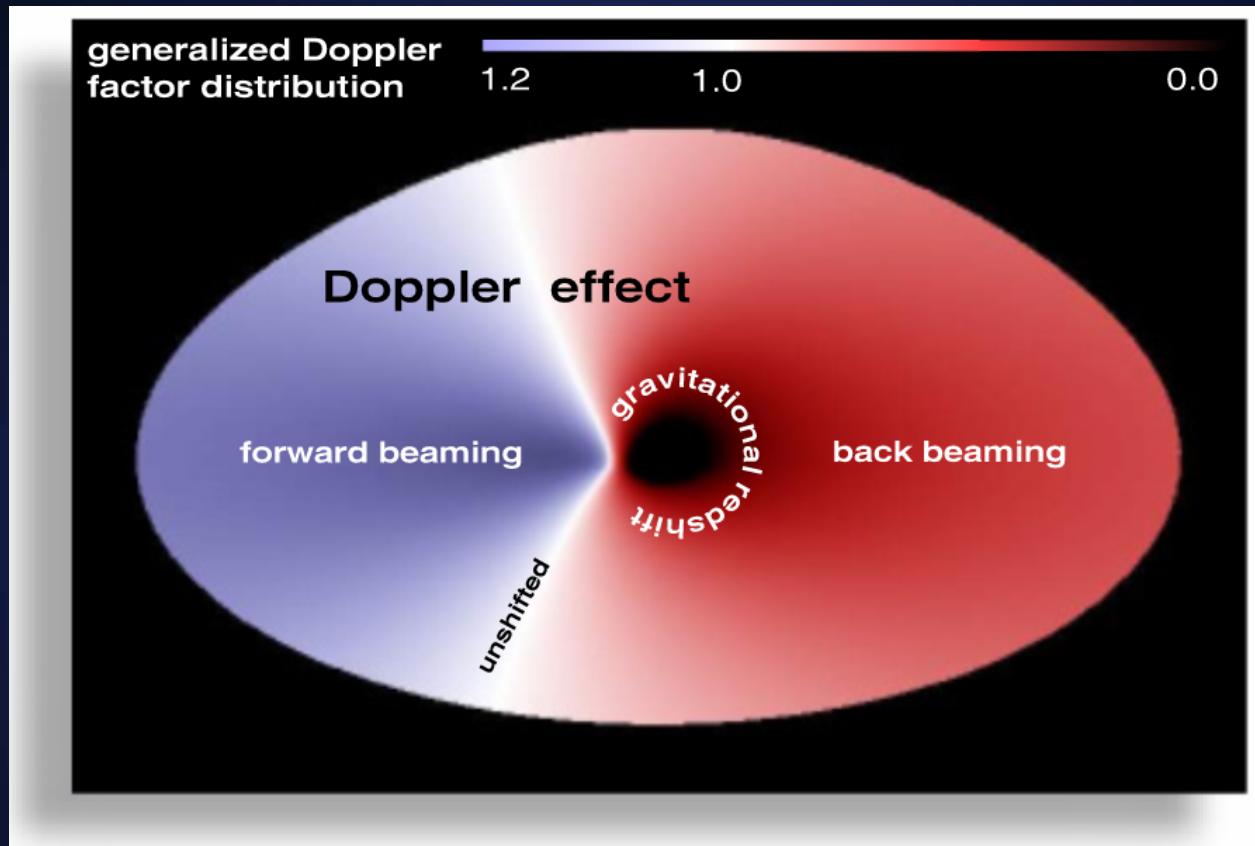
*japanese group*

# black hole - ray tracing



- solving geodesics equation on kerr geometry  
(carter photon momenta, 1968)
- direct integration (3D) or fast mapping via ellipt. integrals (2D)
- photons follow null geodesics of space-time

# black hole - render disk images



$$\begin{aligned} i &= 60^\circ \\ a &= 0.99 \\ r_{in} &= r_H \\ r_{out} &= 30.0 \end{aligned}$$

keplerian kinematics

- classical: doppler effect
- relativistic: beaming (sr) and gravitational redshift (gr)
- fully relativistic generalized doppler factor
- effects influence any emission in black hole systems!

# black hole – emission distribution

$a = 0.1$

$i = 40^\circ$

$r_{in} = r_H = 1.995 r_g$

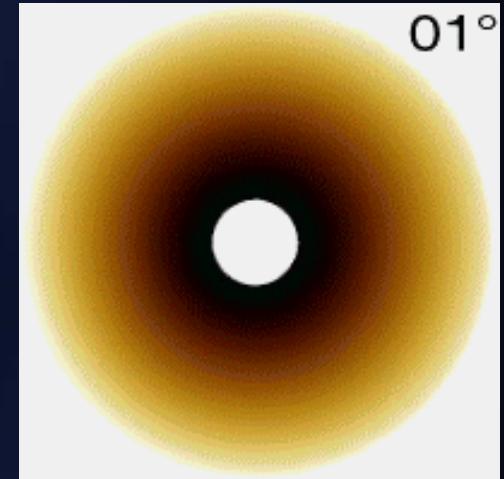
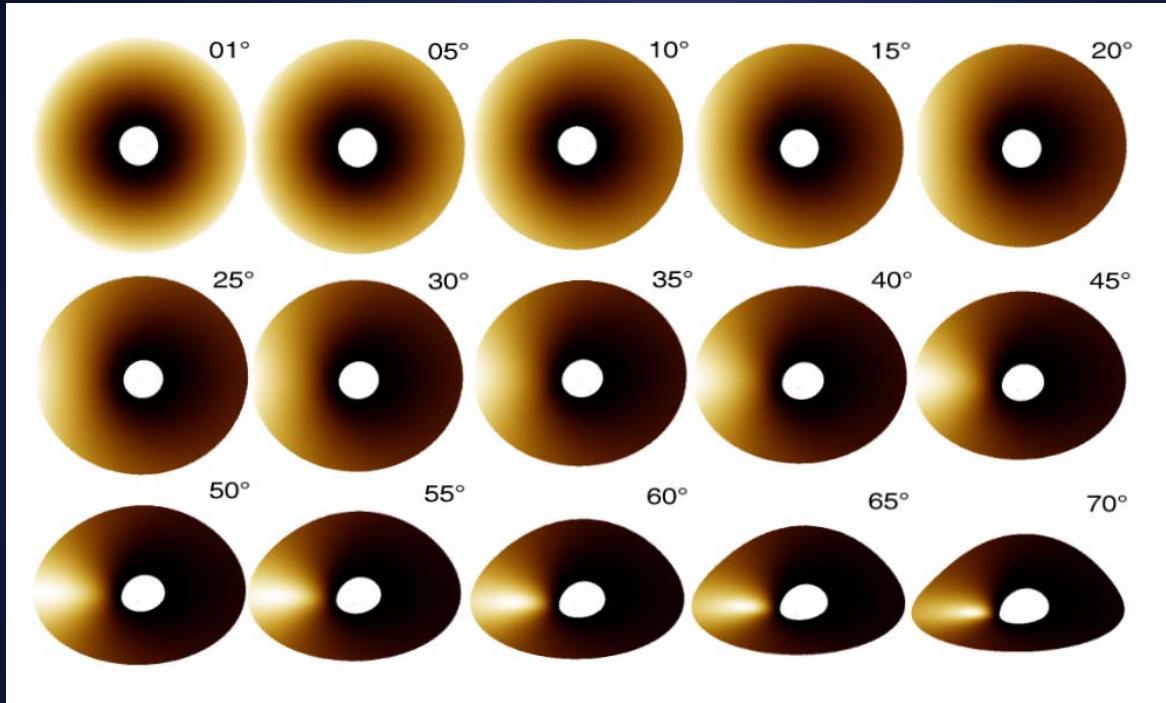
$r_{out} = 30.0 r_g$

$R_t = 6.0 r_g$

*keplerian + drift*

*cut power law*

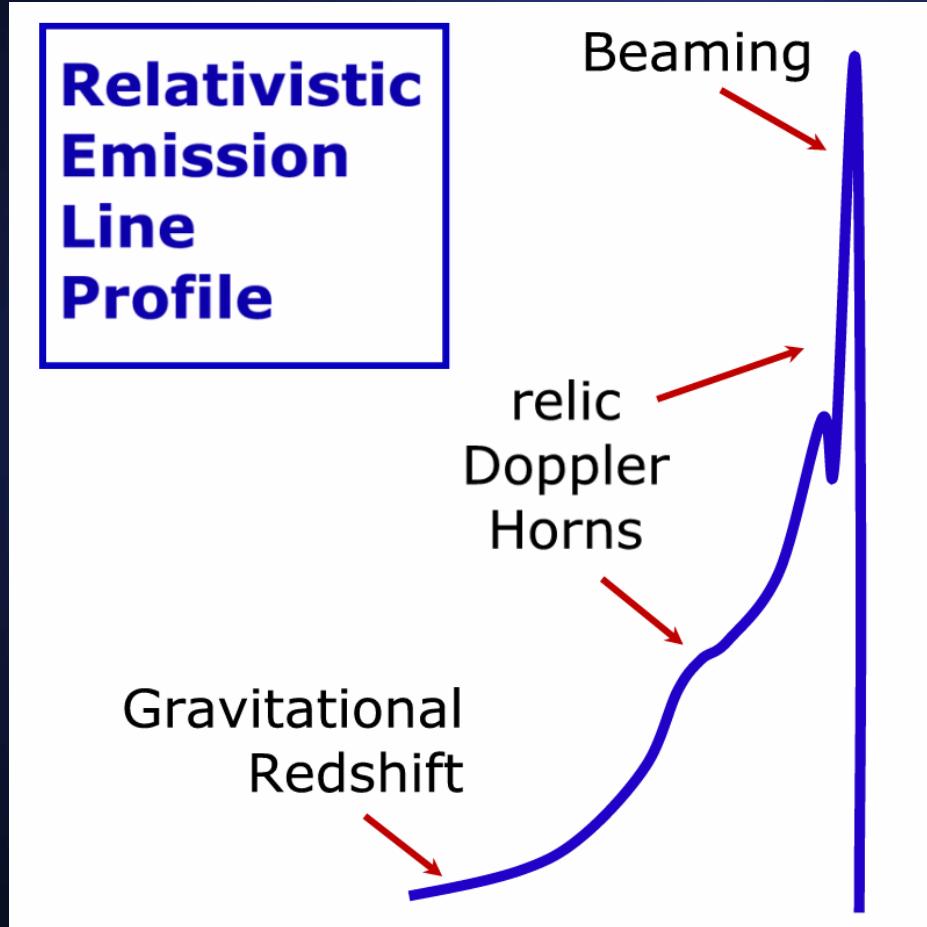
# black hole shadow



- „shadow“ (falcke et al., mpifr) due to gravitational redshift
- grasping with vla scans in near future

*müller 2002,  
[http://www.lsw.uni-heidelberg.de/users/amueler/astro\\_sl.html#kbhrt](http://www.lsw.uni-heidelberg.de/users/amueler/astro_sl.html#kbhrt)*

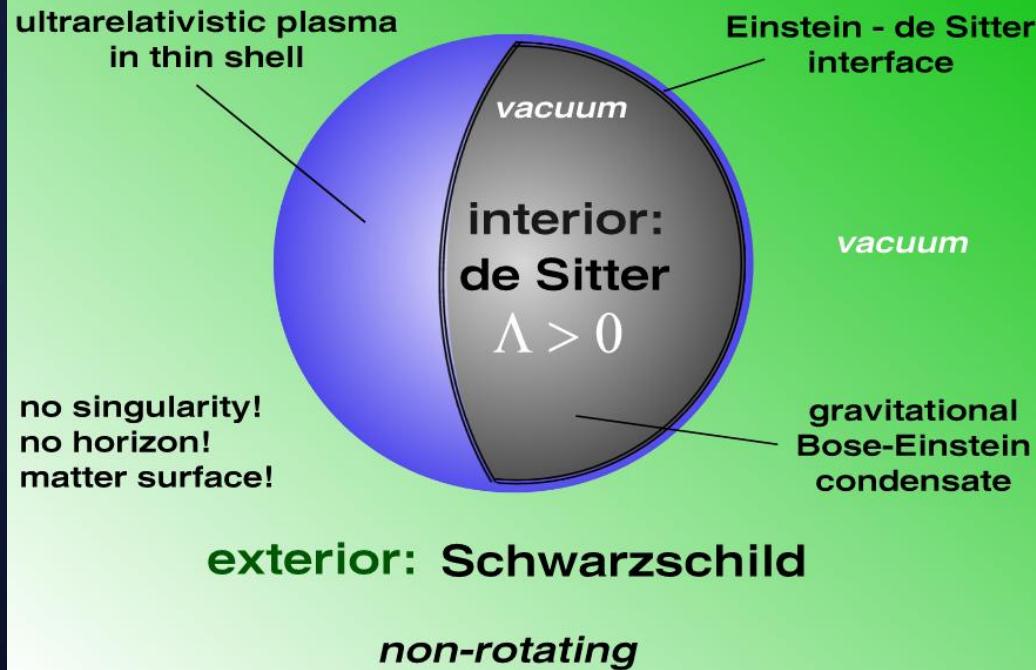
# black hole – emission line diagnostics



- hot ions undergo  $K\alpha$ ,  $K\beta$  transitions
- x-ray emission
- Fe  $K\alpha$  at  $\sim 6.4$  keV dominant
- x-ray data from asca, chandra, xmm
- large parameter space!
  - $\{a, i, r_{in}, r_{out}\}$
  - emissivity law
  - plasma kinematics
- emissivity: power laws (single, double, cut) or gaussian profiles
- line zoo
- sources: seyfert 1s, quasars type 1, microquasars

# black hole crisis – gravastars

## Gravastar

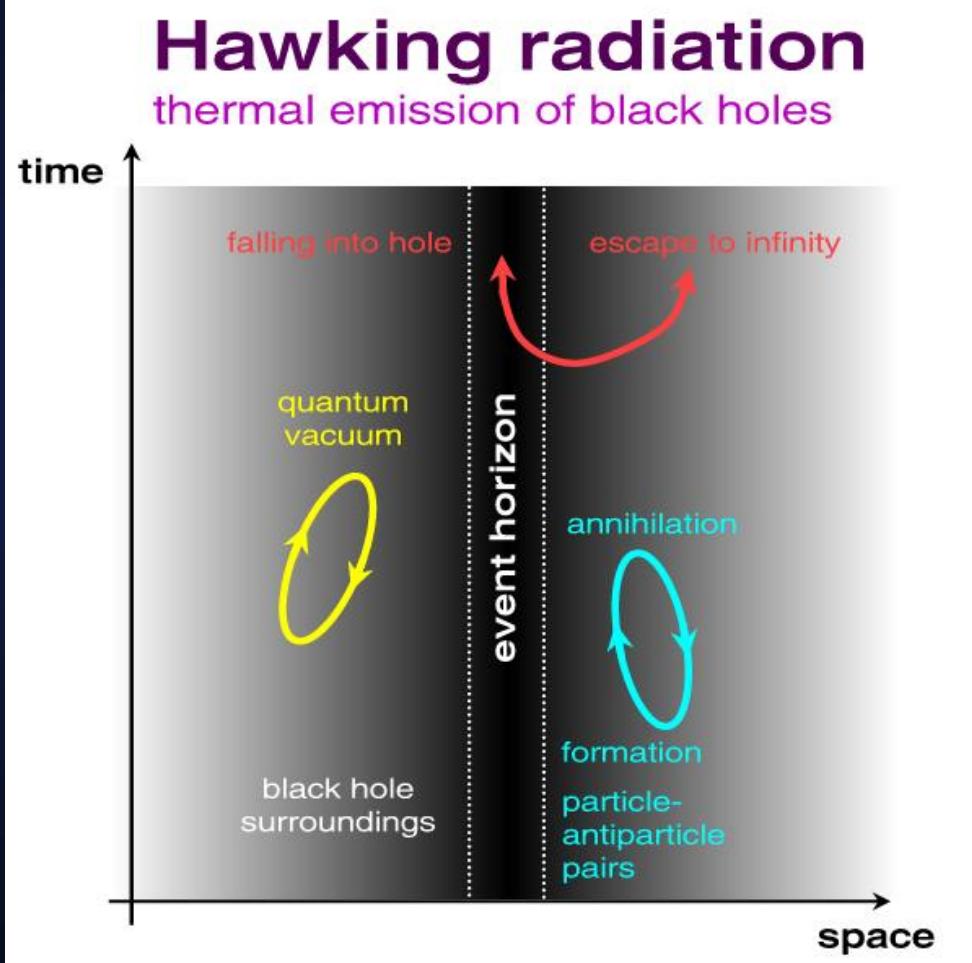


- alternative metric to black hole
- stabilized by antigravitative  $\Lambda$  fluid (dark energy)
- regular!
- no horizon:  
escape velocity  $< c$   
finite redshift  $z_{\text{grav}}$   
redshift factor  $g \sim \varepsilon > 0$

but: **non-rotating**



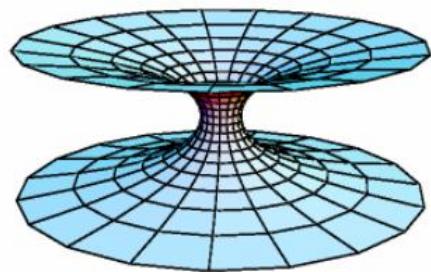
# black hole evaporation



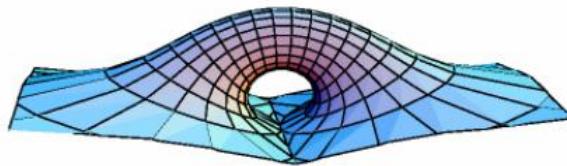
- pair production at horizon (heisenberg uncertainty)
- energy transfer from curved space-time to virtual particle so that it becomes real
- planck emitter with bekenstein-hawking temperature
- **hawking radiation**
- only relevant for very light, non-stellar black holes
- typical decay time scale for stellar bh  $10^{60}$  a
- hawking radiation is analogue to acceleration radiation, the **unruh effect** (equivalence principle)



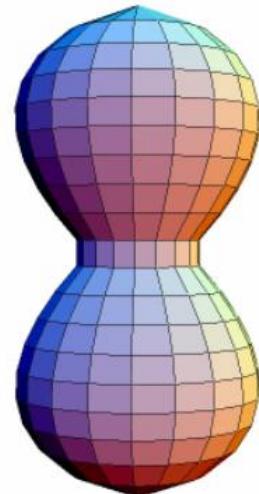
# worm hole - topologies



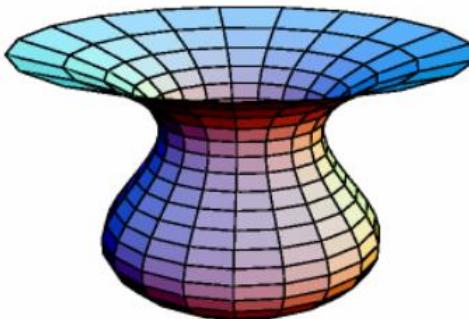
inter-universe



intra-universe



dumbbell: 2 FRW



Minkowski-FRW



# worm hole

- consists of black hole and white hole
- white hole: inverse time-translated black hole
- naked singularity injures cosmic censorship (*penrose*)
- kruskal solution: maximal, analytic extension of schwarzchild solution (kruskal-szekeres coordinates)
- einstein-rosen bridge: channel to other universe?
- stabilization via matter with negative energy density: „exotic matter“ (*morris & thorne 1988*)
- exotic matter generated locally by quantum fields (*hochberg et al. 1997*)
- wormhole may be traversable by humanoid (*kuhfittig 2004*)
- time conjecture hypothesis (*hawking 1992*)
- **never ever observed** in our universe!



# black holes – dynamical horizon

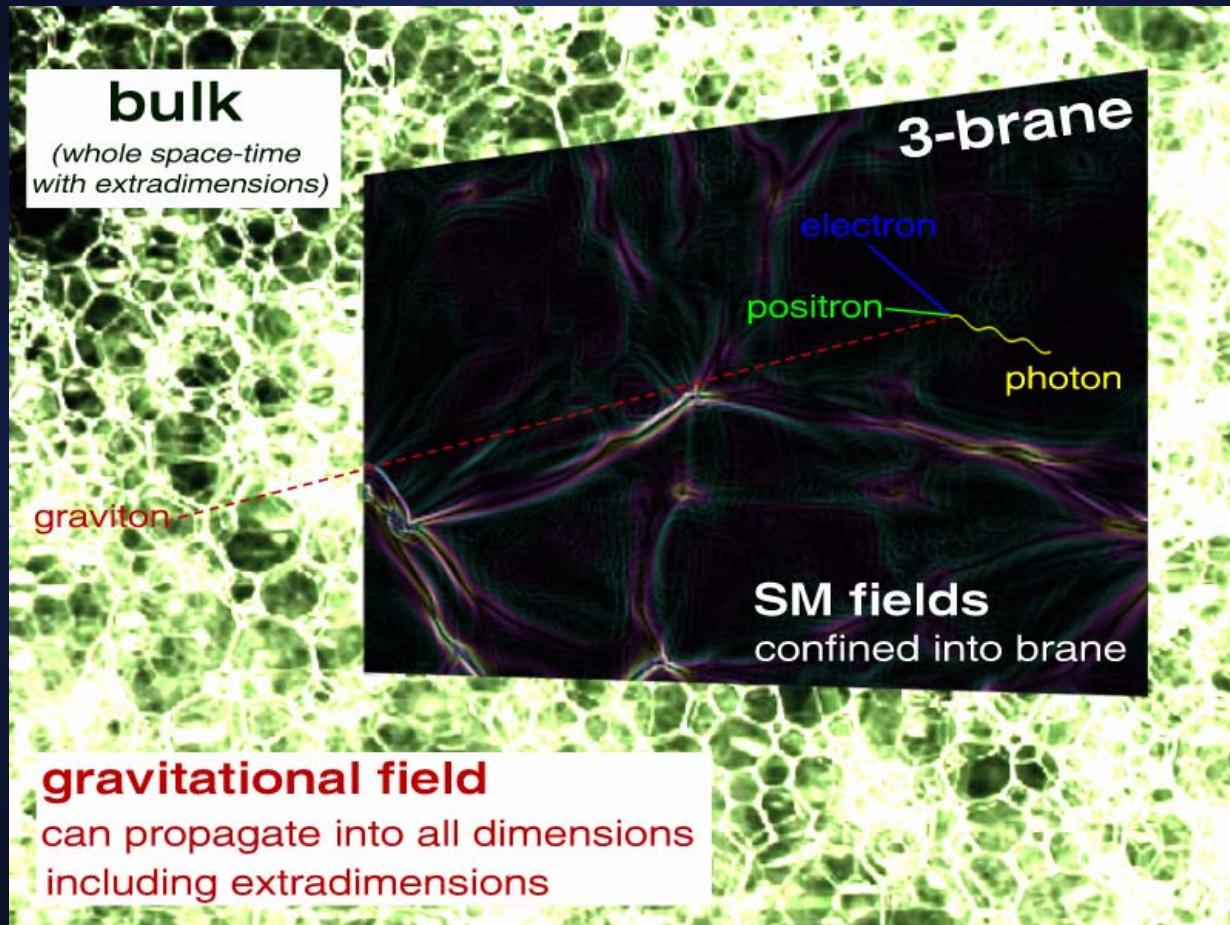
- event horizon: teleological character
- isolated black holes vs. accreting black holes
- new notion: *,dynamical horizon‘*
- growth by infalling matter, radiation, gravitational waves
- use of full non-linear general relativity
- flux equation!
- generalization of black hole mechanics (hawking, 1971)
- application in numerical relativity: simulation of bh-bh merging and gravitational wave output (aei potsdam, germany)

# black holes in string theories

- higher-dimensional generalizations of bh in gr, depending on action/lagrangian
- p-brane has p dimensions
  - 0-brane: point-like black hole
  - 1-brane: black string
  - 2-brane: black brane
- application in particle accelerators?
- new implication for astrophysics:
  - hawking evaporation time-scale shorter with spatial extradimensions!
  - brane cosmology



# black holes in brane worlds



- extradimensions assumed!
- black hole as 3-brane
- TeV quantum gravity: reduced planck scale
- formation of mini black holes
- decay via hawking radiation on short time scale,  $10^{-24}$  s
- **not yet observed!**

cavaglia 2002

brax & bruck, hep-th/0303095



# black holes on the web

[http://www.lsw.uni-heidelberg.de/users/amueller/astro\\_sl.html](http://www.lsw.uni-heidelberg.de/users/amueller/astro_sl.html)

more details, more formulae, more images...

have fun!

this talk is available as powerpoint and postscript

[http://www.lsw.uni-heidelberg.de/users/amueller/astro\\_ppt.html](http://www.lsw.uni-heidelberg.de/users/amueller/astro_ppt.html)

have a look into my german web dictionary for astrophysics

[http://www.lsw.uni-heidelberg.de/users/amueller/astro\\_ppt.html](http://www.lsw.uni-heidelberg.de/users/amueller/astro_ppt.html)